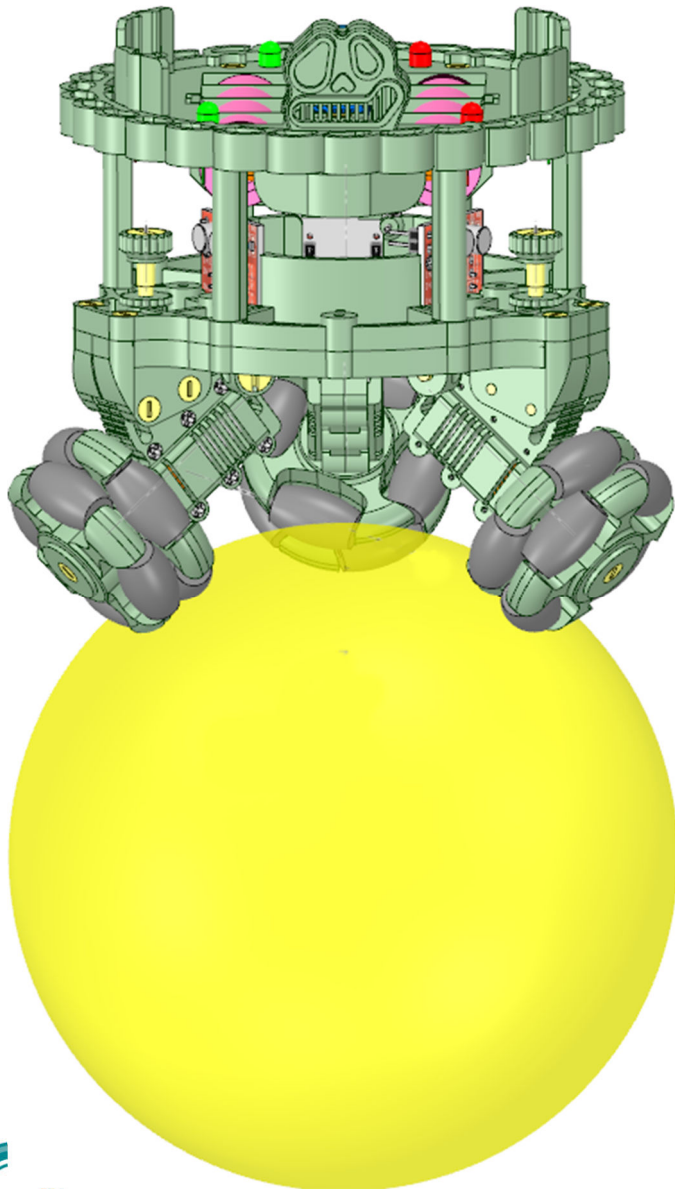
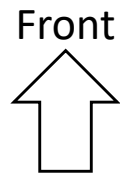


# Ball Balancing Robot

## Calibration



# Ball Balancing Robot Motor Cal.



Left Wheel

Right Wheel

Motor 'A'		
D10	PWM	Direction
0	49-255	Anti-clock
1	223-0	Clockwise

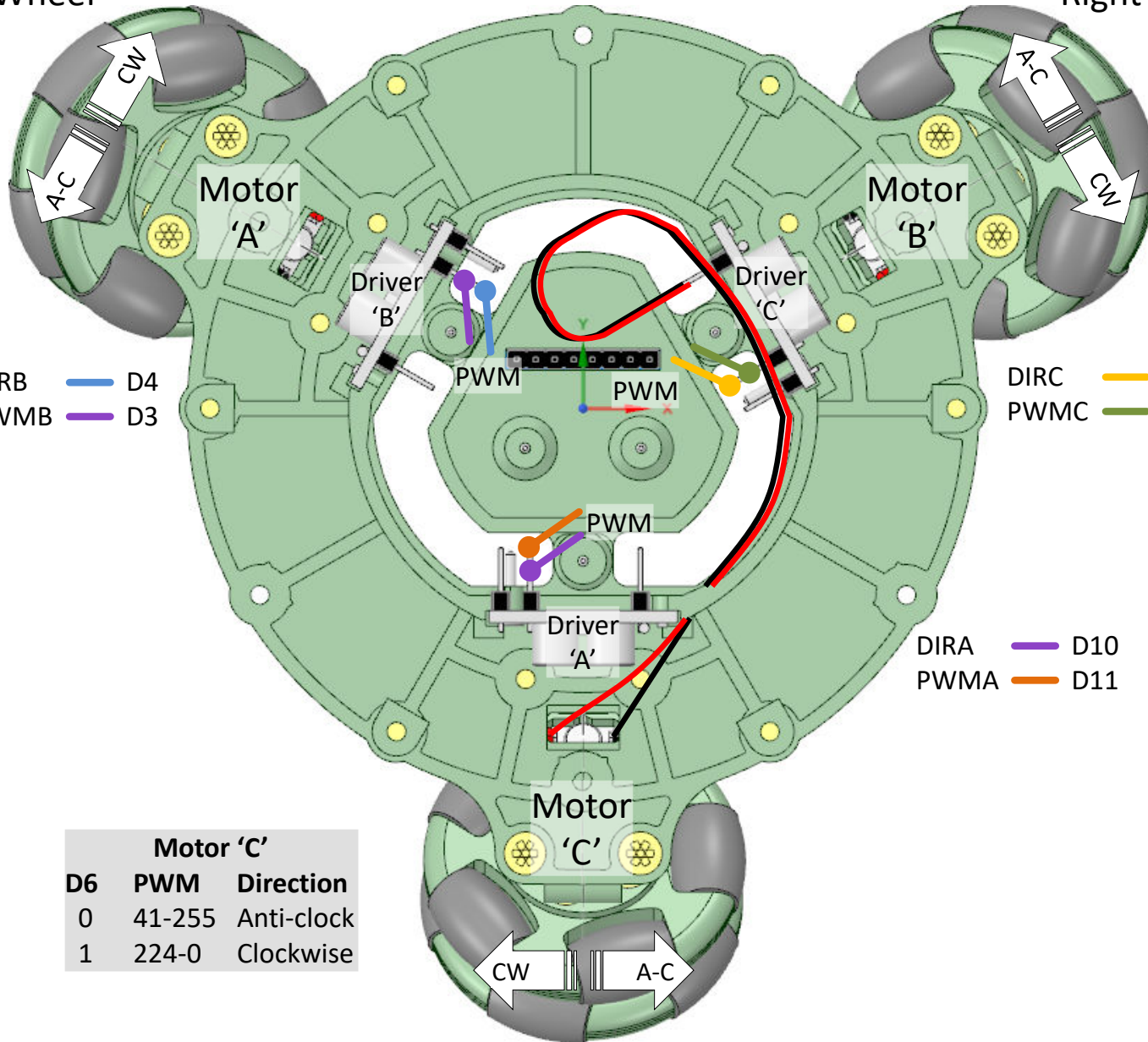
Motor 'B'		
D4	PWM	Direction
0	36-255	Anti-clock
1	233-0	Clockwise

DIRB — D4  
PWMB — D3

DIRC — D6  
PWMC — D9

DIRA — D10  
PWMA — D11

Motor 'C'		
D6	PWM	Direction
0	41-255	Anti-clock
1	224-0	Clockwise



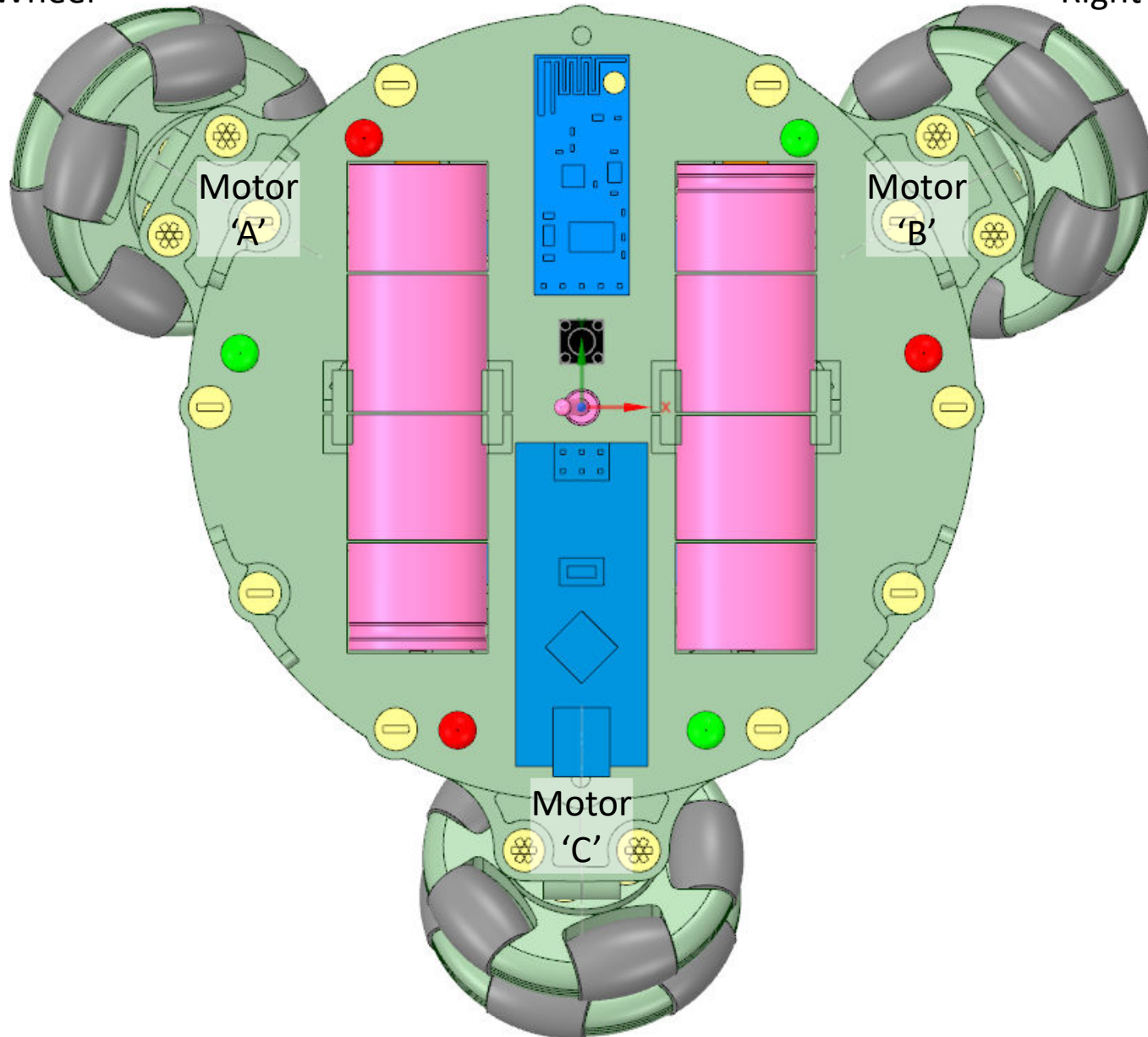
Rear Wheel

Ball Balancing Robot  
Hips Cal.

Left Wheel

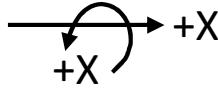
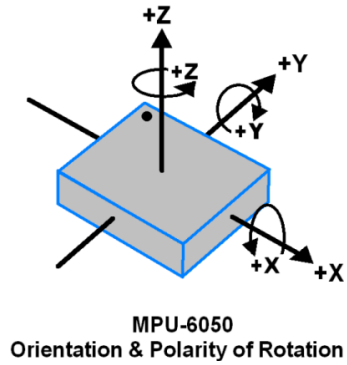
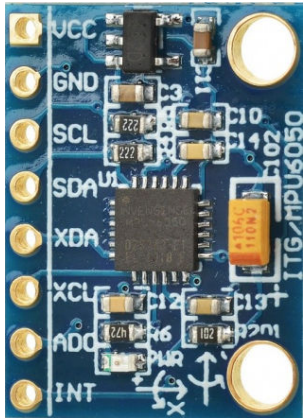


Right Wheel

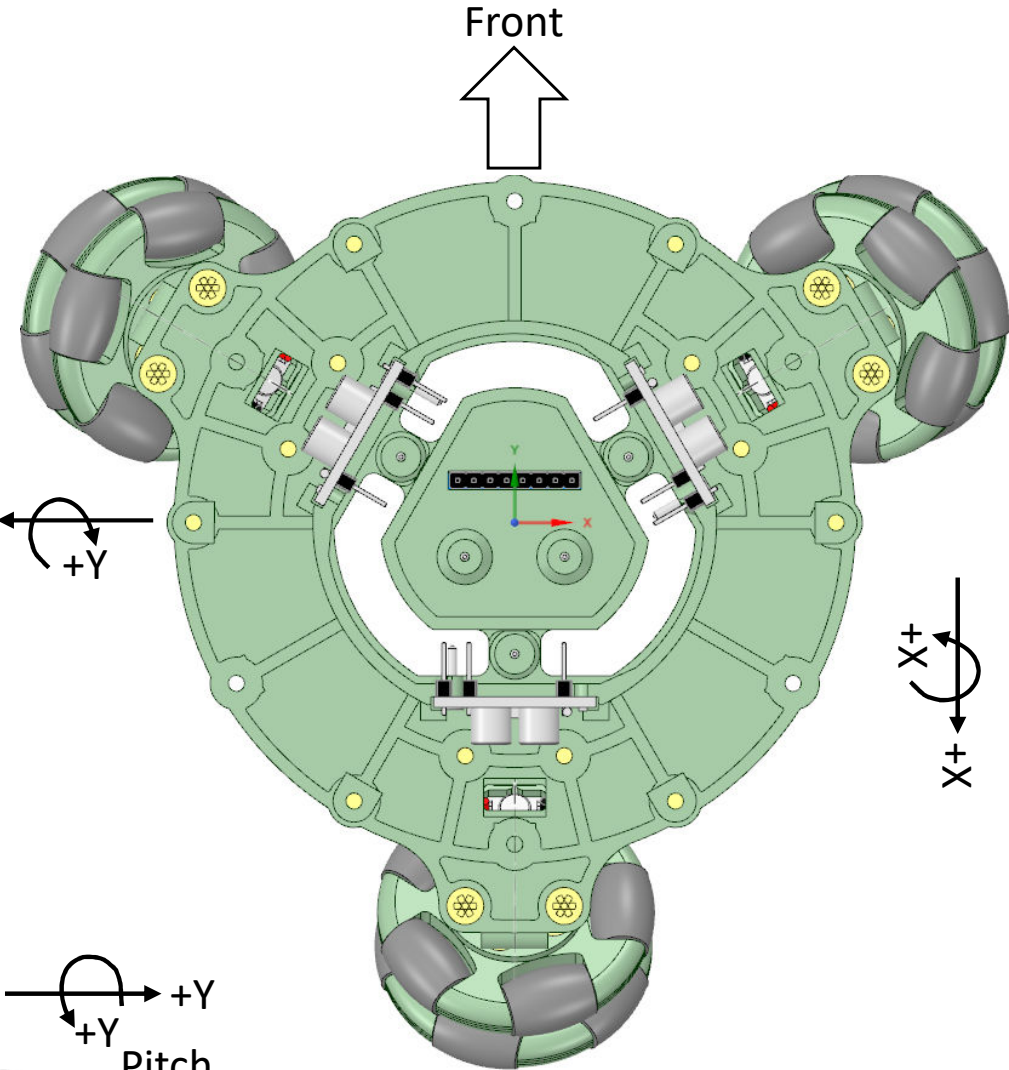
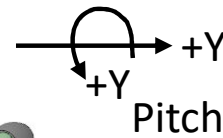
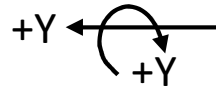
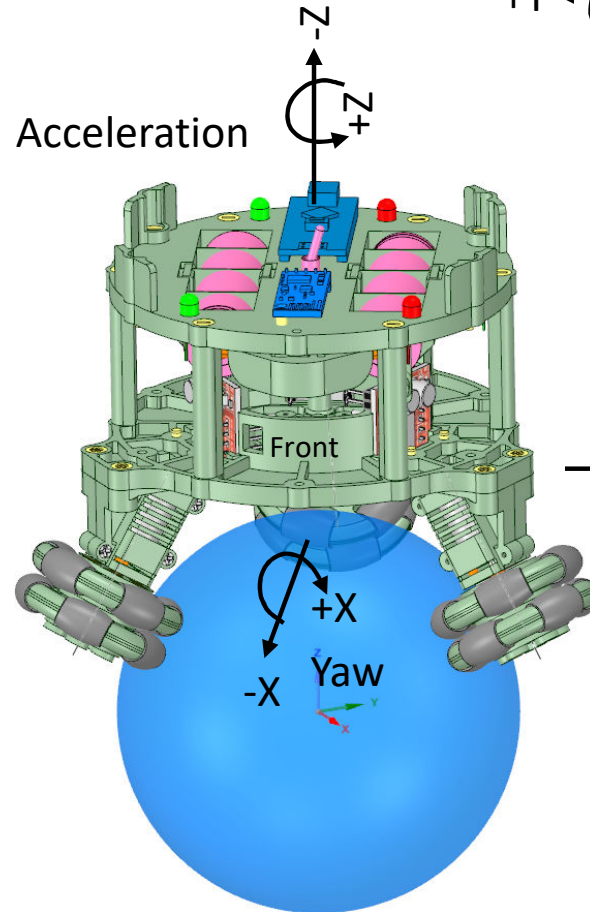
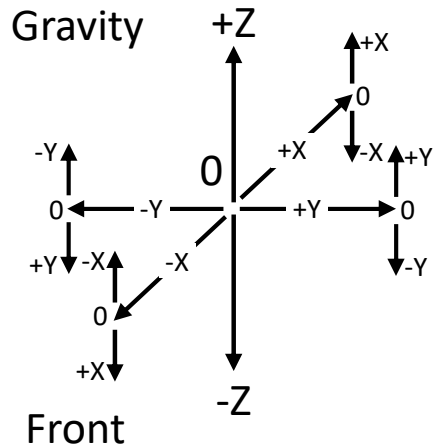


Rear Wheel

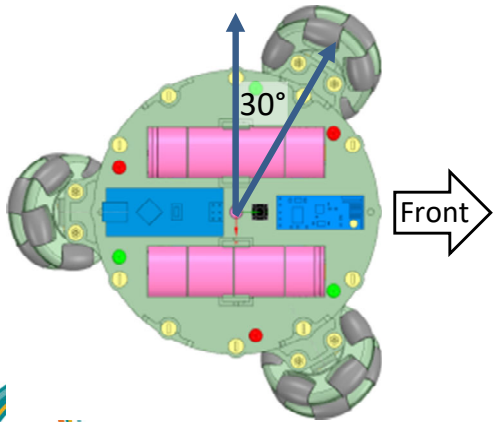
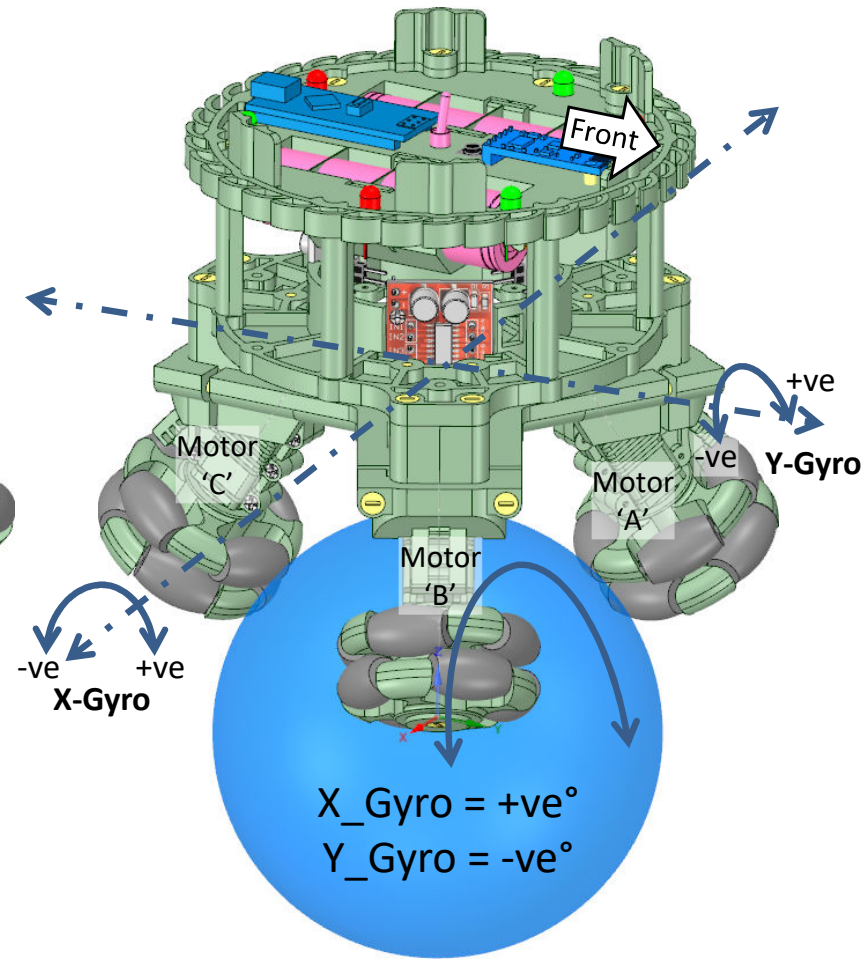
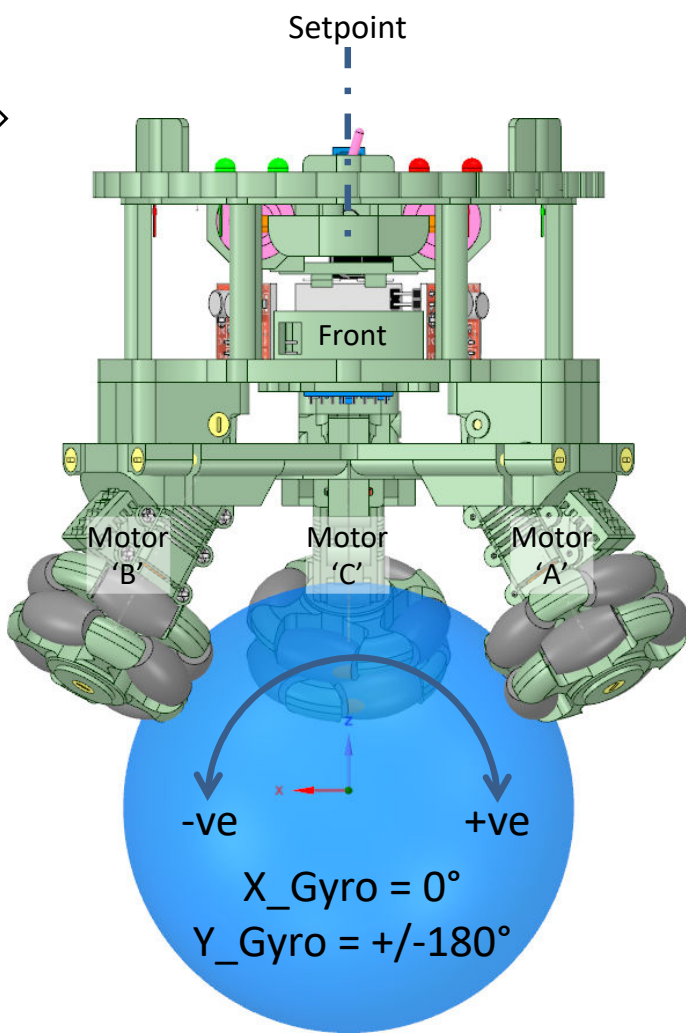
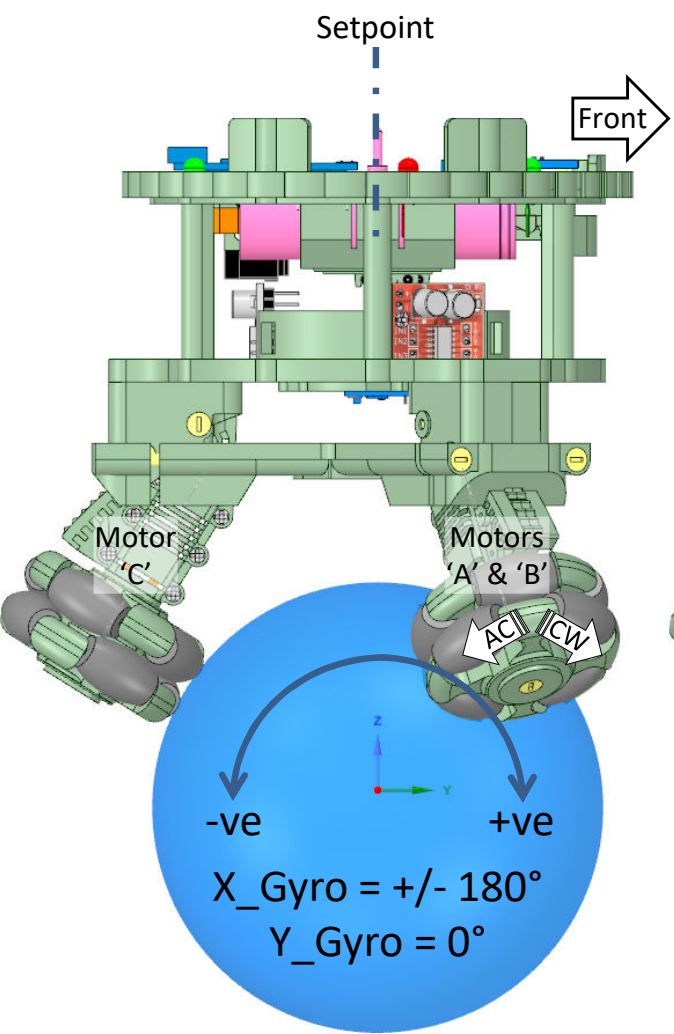
# MPU-6050 Orientation



Acceleration



Gyroscopes are set at +/-250 °/sec FSD.  
 Hence at 32,767 FSD; rotation of 1 °/sec = 131.  
 To convert this to a gyro angle we use the time between readings.  
 On 10 ms cycle we would accumulate a count of 1310 over a 100  
 cycles when rotating at 1 °/sec.  
 So delta angle per 10ms cycle = gyro rate \* 0.00007633



Gyro X & Y angles to Motor clockwise drive relationships:

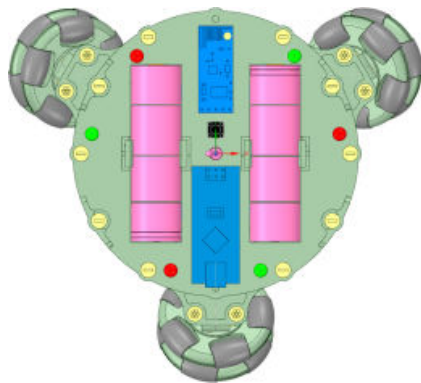
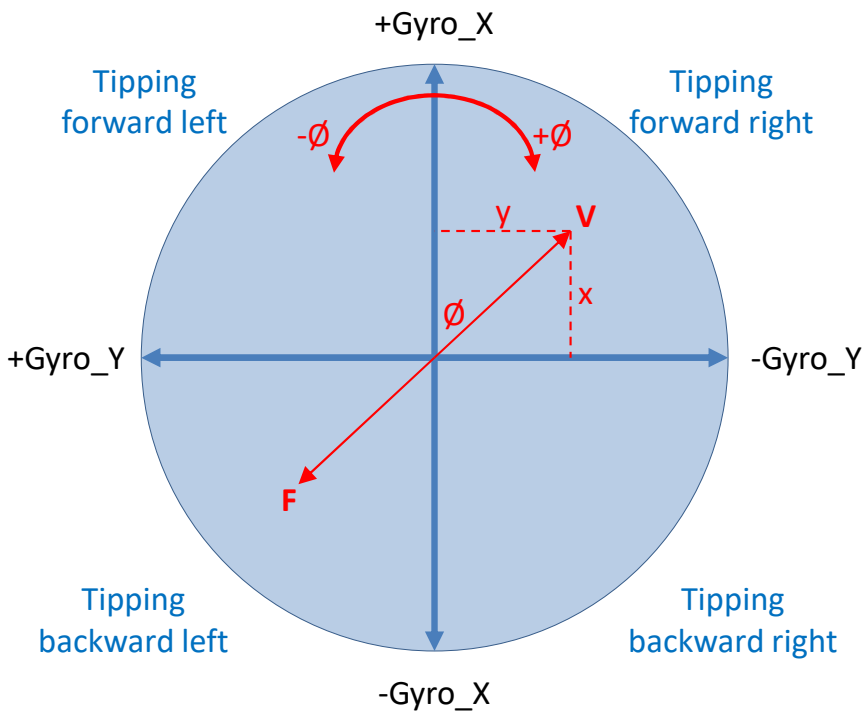
$$\text{Motor A}^{\text{CW}} = -(X_{\text{Gyro}} * \sin(30^\circ)) + (Y_{\text{Gyro}} * \sin(60^\circ)) = -X_{\text{Gyro}} * 0.5 + Y_{\text{Gyro}} * 0.86603$$

$$\text{Motor B}^{\text{CW}} = (X_{\text{Gyro}} * \sin(30^\circ)) + (Y_{\text{Gyro}} * \sin(60^\circ)) = X_{\text{Gyro}} * 0.5 + Y_{\text{Gyro}} * 0.86603$$

$$\text{Motor C}^{\text{CW}} = Y_{\text{Gyro}}$$

Note: here we are calling the Pitch gyro X\_Gyro and Yaw gyro Y\_Gyro to be consistent with the accelerometer values, which are used in the code for gyro drift correction.

# Movement angles and vectors



If +X & -Y then:  $\phi^{0 \text{ to } +90} = 57.2958 * \tan^{-1} (y/x)$

If +X & +Y then:  $\phi^{0 \text{ to } -90} = 57.2958 * \tan^{-1} (y/x)$

If -X & -Y then:  $\phi^{90 \text{ to } +180} = 180^\circ - (57.2958 * \tan^{-1} (y/x))$

If -X & +Y then:  $\phi^{90 \text{ to } -180} = -180^\circ + (57.2958 * \tan^{-1} (y/x))$

Tilt  $V = \text{sqrt}(\text{sq}(x) + \text{sq}(y))$  V is always +ve

Driving force vector  $F == \text{PID}(-V)$

F needs to drive in opposite direction to V, so

If +X & -Y then:  $\phi^{90 \text{ to } -180} = -180^\circ + (57.2958 * \tan^{-1} (y/x))$

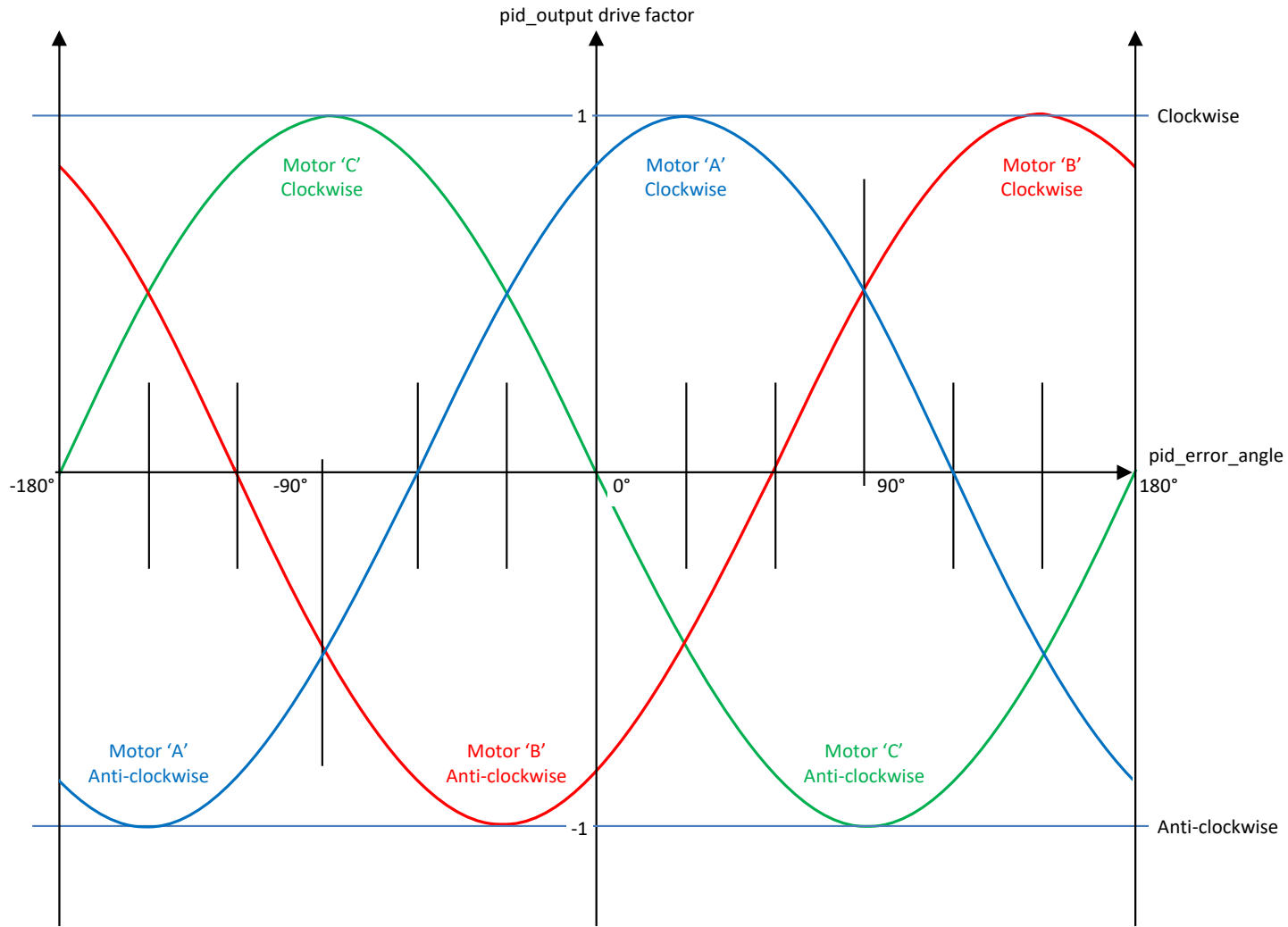
If +X & +Y then:  $\phi^{90 \text{ to } +180} = 180^\circ - (57.2958 * \tan^{-1} (y/x))$

If -X & -Y then:  $\phi^{0 \text{ to } -90} = -(57.2958 * \tan^{-1} (y/x))$

If -X & +Y then:  $\phi^{0 \text{ to } +90} = -(57.2958 * \tan^{-1} (y/x))$

Where 1 radian = 57.2958 degrees

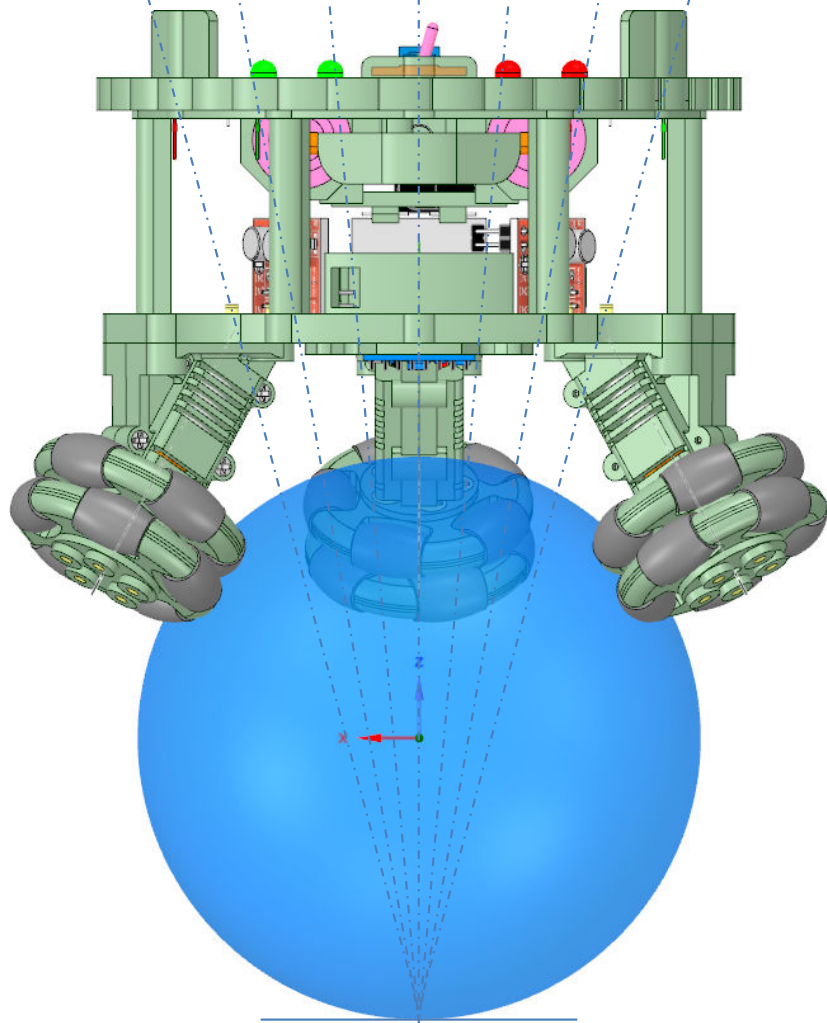
# Motor drive factors $\gamma$ error angle



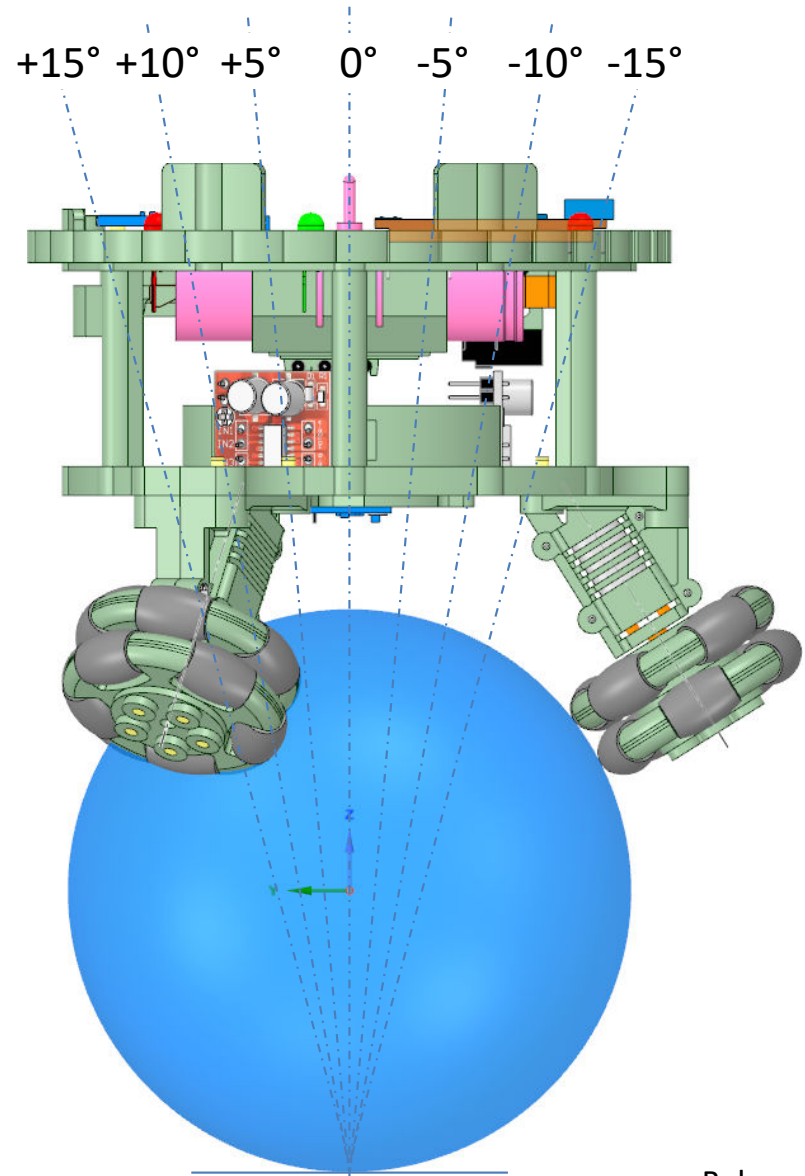
# Balancing Gains

'P' term = Err \* 17  
 0 ← → 255

← +15° +10° +5° 0° -5° -10° -15° →  
 -angle\_gyroY +angle\_gyroY



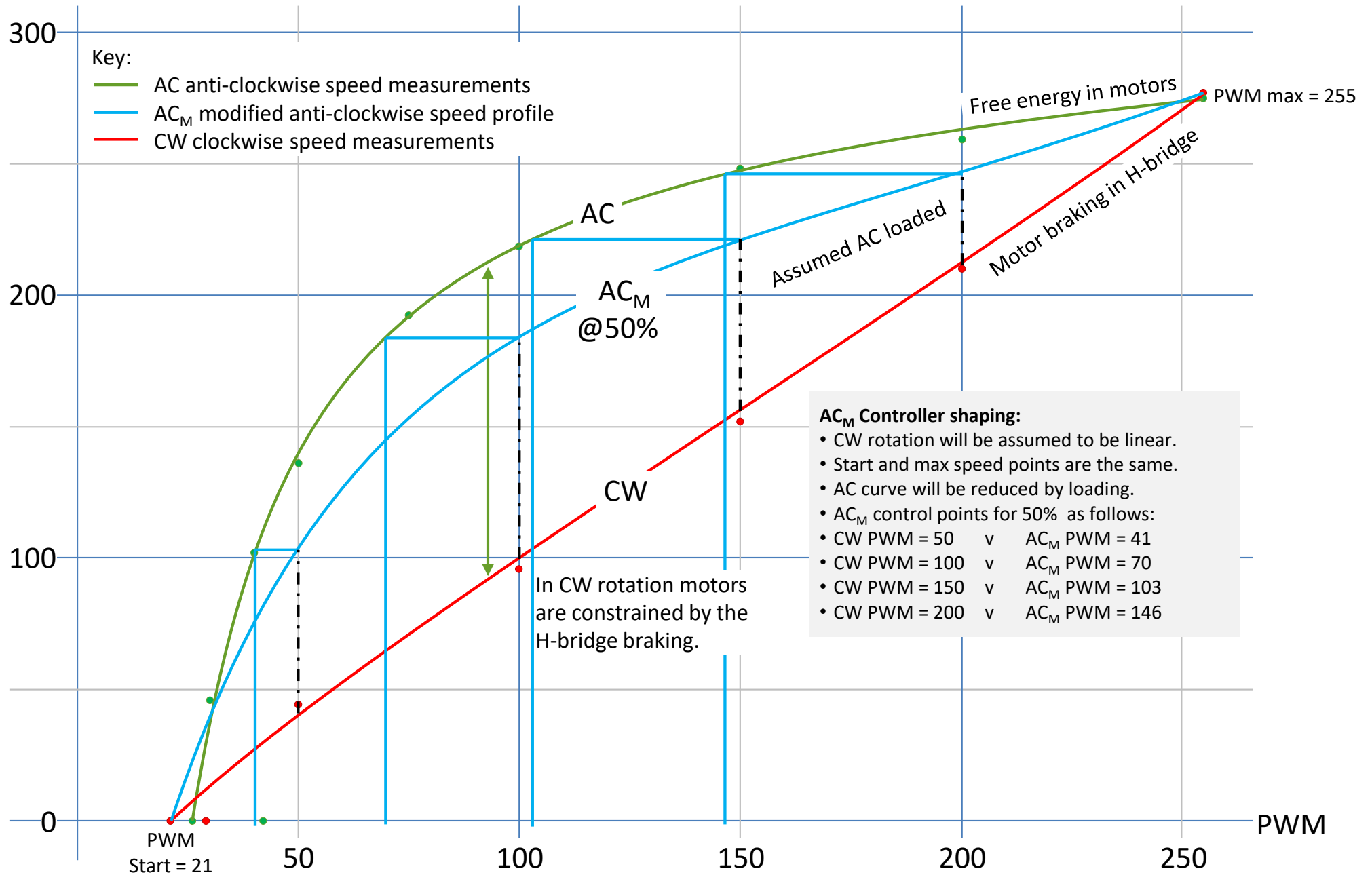
$$\text{pid\_outputX} = \text{pid\_p\_gain} * \text{pid\_error\_tempX}$$



BalanceBot Gains:  
 pid\_p\_gain = 8.0  
 pid\_i\_gain = 0.5  
 pid\_d\_gain = 5.0



# RPM @ 50 counts of ball rotation



Motor speed curves v PWM

# Motor PWM Demand v Power chart

